

Strong Coupling of a Mechanical Oscillator and a Single Atom

K. Hammerer,^{1,5} M. Wallquist,^{1,5} C. Genes,¹ M. Ludwig,² F. Marquardt,² P. Treutlein,³
P. Zoller,^{1,5} J. Ye,^{4,5} and H. J. Kimble⁵

¹*Institute for Theoretical Physics, University of Innsbruck, and Institute for Quantum Optics and Quantum Information, Austrian Academy of Sciences, Technikerstrasse 25, 6020 Innsbruck, Austria*

²*Department of Physics, Center for NanoScience, and Arnold Sommerfeld Center for Theoretical Physics, Ludwig-Maximilians-Universität München, Theresienstrasse 37, D-80333 Munich, Germany*

³*Max-Planck-Institute of Quantum Optics and Department of Physics, Ludwig-Maximilians-Universität München, Schellingstrasse 4, D-80799 Munich, Germany*

⁴*JILA, National Institute of Standards and Technology and University of Colorado, Boulder, Colorado 80309-0440, USA*

⁵*Norman Bridge Laboratory of Physics 12-33, California Institute of Technology, Pasadena, California 91125, USA*

(Received 7 May 2009; published 6 August 2009)

We propose and analyze a setup to achieve strong coupling between a single trapped atom and a mechanical oscillator. The interaction between the motion of the atom and the mechanical oscillator is mediated by a quantized light field in a laser driven high-finesse cavity. In particular, we show that high fidelity transfer of quantum states between the atom and the mechanical oscillator is in reach for existing or near future experimental parameters. Our setup provides the basic toolbox from atomic physics for coherent manipulation, preparation, and measurement of micromechanical and nanomechanical oscillators.

DOI: 10.1103/PhysRevLett.103.063005

PACS numbers: 37.30.+i, 07.10.Cm, 42.50.Dv

Recent experiments with micromechanical and nanomechanical oscillators coupled to the optical field in a cavity are approaching the regime where quantum effects dominate [1–3]. In light of this progress, the question arises to what extent the quantized motion of a mesoscopic mechanical system can be coherently coupled to a microscopic quantum object [4–9], the ultimate challenge being strong coupling to the motion of a single atom. A direct mechanical coupling involves scale factors $\sqrt{m/M} \sim 10^{-7}$ – 10^{-4} , the mass ratio of the atom m and the mechanical oscillator M [4]. It is hence difficult to achieve the strong coupling regime.

In this Letter we show, however, that strong coupling can be realized between a single trapped atom and an optomechanical oscillator. The coupling between the motion of a membrane [10]—representing the mechanical oscillator—and the atom is mediated by the quantized light field in a laser driven high-finesse cavity. Remarkably, in this setup a coherent coupling for single atom and membrane exceeding the dissipative rates by a factor of 10 is within reach for present or near future experimental parameters [11]. Entering the strong coupling regime provides a quantum interface allowing the coherent transfer of quantum states between the mechanical oscillator and atoms, opening the door to coherent manipulation, preparation, and measurement of micromechanical objects via the well-developed tools of atomic physics.

We propose and analyze a setup which combines the recent advances of micromechanics with membranes in optical cavities [10] and cavity QED with single trapped atoms [11] [see Fig. 1(a)]. We consider a membrane placed in a laser driven high-finesse cavity representing the optomechanical system with radiation pressure coupling. In

this setup the motion of the membrane manifests itself as a dynamic detuning of cavity modes. For a cavity mode driven by a detuned laser this translates into a variation of the intensity of the intracavity light field. In addition, we assume that this intracavity field provides an optical lattice as a trap for a single atom. Thus for the setup of Fig. 1(a) the motion of the membrane will be coupled via the dynamics of the optical trap to the motion of the atom, and vice versa. This coupling is strongly enhanced by the cavity finesse which is a key ingredient in achieving the strong coupling regime.

In the following we are interested in a configuration which—after integrating out the internal cavity dynamics—realizes a coupled oscillator dynamics *linear* in the displacements of atom and membrane ($\hbar = 1$)

$$H = \omega_m a_m^\dagger a_m + \omega_{at} a_{at}^\dagger a_{at} - G(a_{at} + a_{at}^\dagger)(a_m + a_m^\dagger). \quad (1)$$

The first and second terms are the Hamiltonians of the bare micromechanical oscillator and the harmonic motion of the trapped atom, respectively. We adopt the notation $x_\mu \equiv \ell_\mu(a_\mu + a_\mu^\dagger)$ and p_μ for the position and momentum operators (along the cavity axis) with $\mu \equiv (m, at)$ for the membrane and atom, respectively, and a_μ are annihilation operators. Both atom and mechanical oscillator are prepared close to their respective ground states, and their oscillator lengths are denoted by $\ell_m = \sqrt{\hbar/2M\omega_m}$ and $\ell_{at} = \sqrt{\hbar/2m\omega_{at}}$ with $\ell_m \ll \ell_{at}$ in view of $M \gg m$, and we assume a near resonance condition $\omega_m \approx \omega_{at}$ of the mechanical and atomic oscillation frequencies. The system dynamics will obey a master equation

$$\dot{\rho} = -i[H, \rho] + (L_c + L_{at} + L_m)\rho, \quad (2)$$

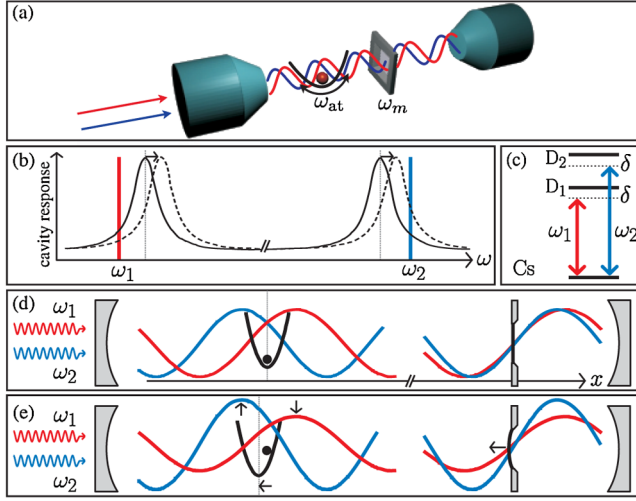


FIG. 1 (color online). (a) Strong coupling of the motion of a single atom to a vibrational degree of freedom of a micron-sized membrane can be achieved in a two mode cavity (for details see text). (b) Cavity response as a function of frequency. Two cavity modes are driven by two lasers of frequencies ω_1 and ω_2 , with red and blue detuning, respectively. (c) The two frequencies drive two atomic transitions, e.g., the $D_{1,2}$ lines of Cs, both with red detuning, causing ac Stark shift of the ground state. (d) (Left-hand side) The atom is trapped in the potential from the two optical lattices. (Right-hand side) The membrane is placed at a point of steepest slope of the intensity profiles. (e) A small displacement of the membrane will shift the cavity resonances [cf. dashed line in (b)] resulting in a spatial shift of the trap potential for the atom, and thus an effective linear atom-membrane coupling as in Eq. (1).

where the three Liouvillian terms describe dissipation via cavity decay, atomic momentum diffusion due to spontaneous emission, and thermal heating of the membrane, respectively. Our goal is to obtain a coupling G much larger than the rates of decoherence.

A strong effective coupling as in Eq. (1) is obtained in a configuration involving two cavity modes (Fig. 1). The two modes are driven by lasers of frequencies ω_1 and ω_2 , respectively, where the first (second) laser is tuned to the red (blue) side of its respective cavity resonance [Figs. 1(b) and 1(c)]. Both lasers provide red-detuned optical lattices for the atom with wave vectors $k_1 \neq k_2$. A single atom is trapped in one of the wells of the combined potential of the two lattices (Fig. 1(d)). The particular well within the optical lattice array is chosen such that each of the two potentials has close to maximal but opposite slope at the equilibrium position \bar{x}_{at} of the atom. The membrane in turn is positioned at \bar{x}_m halfway between a field node and an antinode, with similar slope for both modes, where the linear optomechanical coupling is maximal [10]. A small displacement of the membrane will thus shift the cavity resonances [cf. dashed line in Fig. 1(b)]. Accordingly, one driving laser will come closer to resonance, the other one farther off resonance. This will in turn make one of the lattice potentials deeper, the other one shallower, giving

rise to a *spatial shift* of the atomic trapping potential proportional to x_m [Fig. 1(e)], resulting in an overall $\sim x_{at}x_m$ coupling as in Eq. (1).

Before we analyze this setup in detail, we note that for a *single* standing-wave cavity mode a displacement of the membrane x_m results in a change of the potential *depth* and thus a *parametric* coupling of the atom to the motion of the membrane of the type $\sim x_m x_{at}^2$. This parametric coupling, which is in principle present also in the proposed two mode setup, will be smaller than the linear coupling in Eq. (1) by at least a Lamb-Dicke factor $\eta = k_1 \ell_{at} \ll 1$ and can be neglected here.

Atom-cavity interaction.—The optical potential along the cavity axis seen by the atom is $V(x) = U_0(u_1(x)A_1^\dagger A_1 + u_2(x)A_2^\dagger A_2)$, where $u_i(x) = \sin^2(k_i x)$ and A_i is a photon destruction operator for field modes $i = 1, 2$. We assume for simplicity that each of the cavity fields generates the same ac Stark shift $U_0 = \frac{\Omega_0^2}{\delta}$ per photon, where Ω_0 is the vacuum Rabi frequency and $\delta < 0$ is the detuning from atomic resonance (see Fig. 1). In our effective 1D model, transverse confinement is naturally provided by the Gaussian intensity profile of the cavity fields. Consider the case where both cavity fields are driven so that we have a large intracavity amplitude α , which we choose to be equal and real for both cavity modes. Expanding the potential in powers of this amplitude yields $V(x) \approx U_0 \alpha^2 u(x) + U_0 \alpha [u_1(x)a_1 + u_2(x)a_2 + \text{H.c.}]$, where $u(x) = u_1(x) + u_2(x)$, and we neglected terms of order zero in α . The operators a_i describe amplitude fluctuations around the coherent field α , i.e., $A_i = \alpha + a_i$. The first term $\sim u(x)$ is the effective atomic potential created by the combined effect of the two cavity modes.

In a Lamb-Dicke expansion around the equilibrium position \bar{x}_{at} , the potential together with the kinetic energy of the atom combine to $p^2/2m + V(x) \rightarrow \omega_{at} a_{at}^\dagger a_{at} + H_{at,c}$, where $H_{at,c} = g_{at,c} [(a_1 + a_1^\dagger) - (a_2 + a_2^\dagger)] (a_{at} + a_{at}^\dagger)$, and we adopt for the motion of the atom a harmonic approximation with a trap frequency $\omega_{at}^2 = U_0 \alpha^2 u''(\bar{x}_{at})/m$. Here $H_{at,c}$ is the desired linear atom-field coupling at rate $g_{at,c} = U_0 \alpha \eta \theta$, where $\theta = \frac{u'(\bar{x}_{at})}{k_1}$ is a geometrical factor. We assume that the \bar{x}_{at} is chosen such that $\theta \approx 1$.

Membrane-cavity interaction.—As demonstrated [10], vibrational fluctuations of a thin dielectric membrane couple to cavity quadratures according to $H_{m,c} = -g_{m,c} [(a_1 + a_1^\dagger) + (a_2 + a_2^\dagger)] (a_m + a_m^\dagger)$, with an optomechanical coupling $g_{m,c} = \frac{\epsilon_m}{L} \omega_i f_i(\bar{x}_m) \alpha$ ($i = 1, 2$), which we take for simplicity to be the same for both cavity fields. L is the length of the cavity. The geometrical factor $f_i(\bar{x}_m) = 2r \sin(2k_i \bar{x}_m) / \sqrt{1 - r^2 \cos^2(2k_i \bar{x}_m)}$ depends on the membrane amplitude reflectivity r and the equilibrium position \bar{x}_m of the membrane. By a proper choice of \bar{x}_m it is possible to achieve $f_i \approx 2r$ for both fields.

Open system dynamics.—For the combined system of Fig. 1(a) we thus arrive at a Hamiltonian $H = \omega_{at} a_{at}^\dagger a_{at} + \omega_m a_m^\dagger a_m - \Delta (a_1^\dagger a_1 - a_2^\dagger a_2) + H_{at,c} + H_{m,c}$. For the two

cavity fields this Hamiltonian refers to frames rotating at the respective driving laser frequencies ω_i ; see Fig. 1. The laser detunings, $\pm\Delta$, for the two cavity modes are chosen equal in magnitude and opposite in sign. The coherent evolution is accompanied by various decay channels described by a master equation $\dot{W} = -i[H, W] + (L_1 + L_2 + L_{at} + L_m)W$. Using the notation $D[a]W = 2aWa^\dagger - a^\dagger aW - Wa^\dagger a$ to denote a general Lindblad term, we have in particular $L_{1,2}W = \kappa D[a_{1,2}]W$ with a cavity amplitude decay rate κ . Spontaneous emission will inevitably cause momentum diffusion of the atom, which is described by $L_{at}W = \frac{\Gamma_{at}}{2}D[a_{at} + a_{at}^\dagger]W$ and happens at a rate $\Gamma_{at} = \gamma \frac{\Omega_0^2 \alpha^2}{\delta^2} \eta^2 u(\bar{x}_{at}) = \gamma \frac{g_{at,c}^2}{\Omega_0^2} \xi$, where γ is the spontaneous decay rate [12]. The geometrical factor $\xi = \frac{k_1^2 u(\bar{x}_{at})}{u_1'(\bar{x}_{at})^2}$ can be made close to unity by a proper choice of \bar{x}_{at} [13]. Finally, thermal contact of the membrane to the environment at a temperature T is accounted for by $L_mW = \frac{\gamma_m}{2} \times (\bar{n} + 1)D[a_m]W + \frac{\gamma_m}{2} \bar{n}D[a_m^\dagger]W$, where γ_m is the natural linewidth of the mechanical resonance and \bar{n} its mean occupation in thermal equilibrium. The relevant effective decoherence rate of the membrane is $\Gamma_m = \gamma_m \bar{n} \approx \frac{k_B T}{\hbar Q}$ for a mechanical quality factor Q .

Mediated atom-membrane interaction.—We are now in the position to derive the effective cavity-mediated coupling between the single atom and the membrane. Consider the case of far off-resonant drive $|\Delta| \gg g_{at,c}, g_{m,c}$, where fluctuations in cavity quadratures are fast variables and adiabatically follow the dynamics of position fluctuations of atom and membrane. In this dispersive limit the decoherence rate due to cavity decay can be kept small as compared to the strength of coherent evolution by choosing $\frac{\kappa}{\Delta} \ll 1$. We derive an effective master equation for the reduced state of atom and membrane $\rho = \text{tr}_{12}\{W\}$ as given in Eq. (2). The rate of mediated coherent coupling described by the Hamiltonian in Eq. (1) is $G = \frac{2g_{at,c}g_{m,c}(\Delta + \omega_m)}{\kappa^2 + (\Delta + \omega_m)^2} + \frac{2g_{at,c}g_{m,c}(\Delta - \omega_m)}{\kappa^2 + (\Delta - \omega_m)^2}$. The most compelling feature of this cavity-mediated “spring” is that—to the best of our knowledge—this is the first scheme for coupling the motion of a single atom to a massive oscillator which manages to avoid the mass ratio $\sqrt{m/M}$ entering the coupling strength. This ratio necessarily enters any translationally invariant coupling $\sim (x_{at} - x_m)^2$, as it sets the relative magnitude of the cross term $\sim x_{at}x_m$ versus the direct atomic frequency shift term $\sim x_{at}^2$.

Decay of the cavity field gives rise to four channels of decoherence in the effective master equation in Eq. (2), $L_c\rho = \sum_{\sigma=\pm} \frac{\Gamma_c^\sigma}{2} D[J_\sigma]\rho + \frac{\Gamma_c^{-\sigma}}{2} D[J_\sigma^\dagger]\rho$ at rates $\Gamma_c^\pm = \frac{2\kappa(g_{at,c}^2 + g_{m,c}^2)}{\kappa^2 + (\Delta \pm \omega_m)^2}$ with jump operators $J_\pm = \cos(\phi)a_m \pm \sin(\phi)a_{at}$ where $\tan\phi = \frac{g_{at,c}}{g_{m,c}}$. Each jump corresponds to the emission of sideband photons at either side of the two driving lasers and is associated with the creation or annihilation of a quantum in either atom or membrane. For a near resonant system ($\omega_m \approx \omega_{at}$) these two possibilities are indistinguishable, and happen in a coherent fashion.

Strong coupling regime.—We now show that the coupling can be strong enough such that coherent dynamics dominates over the various decoherence processes. In a system described by the effective master equation (2) strong coupling is established by fulfilling the set of conditions $G \gg \Gamma_c^\pm, \Gamma_{at}, \Gamma_m$, in addition to $\omega_{at} = \omega_m$ for a resonant coupling. For a ratio $\frac{\Gamma_c^\pm}{G} \ll 1$, it is necessary to drive the cavity far off-resonant, and it is desirable to keep at the same time a balanced atom-cavity and membrane-cavity coupling $g_{at,c} \approx g_{m,c}$, which is equivalent to

$$\Delta \gg \kappa, \omega_m, \quad \frac{4r}{\pi} \frac{\delta}{\gamma} \frac{\mathcal{F}}{C} \sqrt{\frac{m}{M}} \approx 1, \quad (3)$$

respectively. Here $C = \frac{\Omega_0^2}{\kappa\gamma}$ is the one-atom cooperativity parameter and $\mathcal{F} = \frac{\pi c}{2\kappa L}$ the cavity finesse. Small decoherence due to atomic momentum diffusion, $\frac{\Gamma_{at}}{G} \ll 1$, requires a large cooperativity parameter

$$C \gg \frac{\Delta}{4\kappa}. \quad (4)$$

Finally, thermal decoherence depends on the ambient temperature T of the membrane. It is important to note that there is a natural lower limit for the temperature T which is set by light absorption inside the membrane. If we assume the cavity finesse to be limited by absorption, the power absorbed by the membrane is $P_a \approx \frac{2\pi}{\mathcal{F}} P_c$ for an overall circulating power $P_c = \frac{\hbar\omega_1 c \alpha^2}{L}$ in the two cavity modes. Such an amount of absorbed power will cause an increase of the membrane temperature $\Delta T \approx \frac{1}{k_B \kappa_{th}} P_a$, where κ_{th} is the thermal link of the membrane to its supporting frame which depends on the specific geometry and material properties [14]. While it is not entirely clear how this heating exactly affects the vibrational mode in question, a safe assumption is an equal increase in temperature. For typical parameters (see below), ΔT corresponds to a few kelvin, so that standard cryogenic precooling allows one to reach $T \approx \Delta T$. Under these fairly cautious assumptions we can expect a small thermal decoherence $\frac{\Gamma_m}{G} \ll 1$ as long as

$$\frac{8r^2}{\pi^2} \frac{\kappa_{th}}{\gamma_m} \frac{\hbar\omega_1}{Mc^2} \mathcal{F}^2 \gg \frac{\Delta}{\kappa}. \quad (5)$$

Remarkably, this is independent of circulating power and only implicitly depends on temperature through κ_{th} [15].

Together, Eqs. (3)–(5) ensure the set of conditions for strong coupling $G \gg \Gamma_c^\pm, \Gamma_{at}, \Gamma_m$. Note that the intracavity amplitude α and therefore the absolute time scale of the system are not fixed by Eqs. (3)–(5). These equations actually impose conditions on the properties of the system at the single photon level. The necessary cavity amplitude α , and with it the absolute time scale of the dynamics, will finally follow from the resonance condition $\omega_{at} = \omega_m$.

Example.—We will show now that the interaction between a single Cs atom and a SiN membrane of small effective mass $M = 0.4$ ng mediated by a high-finesse

optical microcavity can enter the strong coupling regime. First, we assume a large cavity finesse of $\mathcal{F} \approx 2 \times 10^5$, which is consistent with a measured value of $\text{Im}(n) \approx 1 \times 10^{-5}$ for the absorption in a SiN membrane inside a cavity [16]. A small cavity waist of $w_0 = 10 \mu\text{m}$ results in a cooperativity parameter of $C = 140$. A ratio of $\frac{\Delta}{\kappa} \approx 18$ satisfies Eqs. (3) and (4). Second, for the mass ratio of $\frac{m}{M} = 6 \times 10^{-13}$ and an amplitude reflectivity $r = 0.45$, we choose a ratio $\frac{\delta}{\gamma} \approx 450$ in order to approximately satisfy the second condition in (3) and at the same time to ease requirements for condition (5). Third, from the data measured in [15] we infer a value of $k_B \kappa_{\text{th}} \approx 10 \text{ nW/K}$ for the dimensions of the membrane ($100 \mu\text{m} \times 100 \mu\text{m} \times 50 \text{ nm}$) = $(l \times l \times d)$ required here. A mechanical quality factor of $Q = 10^7$ and a resonance frequency $\omega_m = 2\pi \times 1.3 \text{ MHz}$ set the left-hand side of Eq. (5) to ~ 45 . Finally, the resonance condition $\omega_{at} = \omega_m$ demands a circulating power $P_c \approx 850 \mu\text{W}$ which will cause heating of $\lesssim 2.5 \text{ K}$ for the given thermal link. We assume the driving laser to be shot noise limited in intensity at the relevant sideband frequencies $\omega_m, 2\omega_m$ and to have kHz linewidth, in order to avoid FM to AM conversion of frequency noise [11]. This is readily achieved at the optical frequencies and μW driving power required here. In order to make a statement about the absolute time scales of the dynamics, we still need to fix the cavity length. For $L = 50 \mu\text{m}$ we find a cavity-mediated coupling $G \approx 2\pi \times 45 \text{ kHz}$ and decoherence rates $\Gamma_c, \Gamma_m, \Gamma_{at} \approx 0.1G$. It is thus indeed possible to enter the strong coupling regime with state-of-the-art experimental parameters.

While being a surprising result on its own, entering the regime of strong coupling holds promise for diverse applications, including for preparation and readout of quantum states of mesoscopic massive oscillators. In the regime $\omega_m = \omega_{at} \gg G$, where the rotating wave approximation can be applied in Eq. (1), the effective dynamics is described by $H_I \approx G(a_m a_{at}^\dagger + \text{H.c.})$ in the interaction picture. This interaction swaps the state of the atom and the membrane after a time $Gt = \frac{\pi}{2}$. Thus, states which are easily created on the side of the atom (e.g., squeezed or Fock states) can be transferred to the membrane. In Fig. 2 we study such a transfer of a squeezed state based on the exact solution of the master equation in Eq. (2). The figure also illustrates the importance of limiting the loss in order to achieve quantum state transfer or readout. The general analysis provided here shows that condition (5) is the principal bottleneck for a reduction of losses. In particular, the ratio $\frac{\kappa_{\text{th}} \mathcal{F}^2}{\gamma_m M}$ might be further increased by improving material properties and nanostructuring, though there will always be an apparent trade off between good mechanical isolation and a large thermal link. Another rather obvious route for improvement is to use a small ensemble of N atoms trapped inside the cavity [17–19], resulting in a \sqrt{N} enhancement of the atom-cavity coupling. However, our

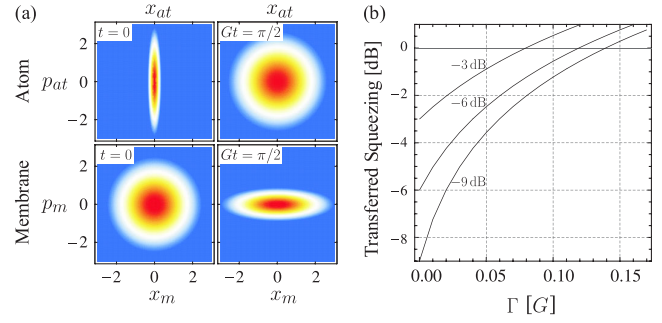


FIG. 2 (color online). (a) Wigner functions of atom and membrane (upper and lower panels, respectively). At $t = 0$ (left-hand panels) the atom is in a squeezed state (9 dB) and the membrane in a thermal state with a mean number of phonons $\bar{n} = 5$. An exact solution of the equation of motion (2) with losses $\Gamma = \Gamma_c, \Gamma_m, \Gamma_{at}$ at rate $\Gamma = 0.1G$ shows that after a time $Gt = \frac{\pi}{2}$ (right-hand panels) the states are exchanged, up to a trivial rotation in phase space by 90° . (b) Squeezing transferred to membrane (maximized over time), versus loss rate Γ , for the indicated values of initial atomic position fluctuations.

main point here is to identify the general conditions for achieving strong coupling of a single atom to a massive mechanical oscillator, and to demonstrate that it is possible to meet these conditions with state-of-the-art systems.

Support by the Austrian Science Fund through SFB FOQUS, by the IQOQI, by the European Union through project EuroSQIP, by NIST and NSF, and by the DFG through NIM, SFB631, and the Emmy-Noether program is acknowledged. M.W., K.H., P.Z., and J.Y. thank H. J. K. for hospitality at Caltech.

- [1] A. Schliesser *et al.*, arXiv:0901.1456v1.
- [2] S. Groeblacher *et al.*, arXiv:0901.1801v1.
- [3] F. Marquardt and S. M. Girvin, arXiv:09050566.
- [4] L. Tian and P. Zoller, Phys. Rev. Lett. **93**, 266403 (2004).
- [5] P. Treutlein *et al.*, Phys. Rev. Lett. **99**, 140403 (2007).
- [6] N. Lambert *et al.*, Phys. Rev. Lett. **100**, 136802 (2008).
- [7] P. Rabl *et al.*, Phys. Rev. B **79**, 041302 (2009).
- [8] C. Genes *et al.*, Phys. Rev. A **77**, 050307 (2008).
- [9] S. Singh *et al.*, Phys. Rev. Lett. **101**, 263603 (2008).
- [10] J. D. Thompson *et al.*, Nature (London) **452**, 72 (2008).
- [11] R. Miller *et al.*, J. Phys. B **38**, S551 (2005).
- [12] We assume that losses to other levels can be excluded.
- [13] For wave numbers $k_{1,2} = \frac{1}{2}(k \pm \delta k)$ the intensity extrema fulfill $k \tan(kx) = -\delta k \tan(\delta kx)$. Points where $\delta kx \approx n\pi$ fulfill $\xi(\bar{x}_{at}), \theta(\bar{x}_{at}) \approx 1$.
- [14] κ_{th} is chosen here such as to have dimensions of Hz.
- [15] B. L. Zink and F. Hellman, Solid State Commun. **129**, 199 (2004).
- [16] D. J. Wilson, C. A. Regal, S. B. Papp, and H. J. Kimble (to be published).
- [17] Y. Colombe *et al.*, Nature (London) **450**, 272 (2007).
- [18] K. W. Murch *et al.*, Nature Phys. **4**, 561 (2008).
- [19] F. Brennecke *et al.*, Science **322**, 235 (2008).